Buoys for Variables in Java

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Abstract: Buoys are a graphical representation of variables. They were invented with the programming language Algol68, but can be used to represent the variables of any programming language. With this notation some otherwise hard problems will become easy to teach and to understand. For Java this includes the following: Of how many parts does a variable consist? What is the difference between a variable of a primitive type and one of a reference type? Since the value of an int-variable is an int-number, why is it that the value of a String-variable is *not* a String-object? What is the difference between the operation == and the method equals? What is the difference between an *empty array* and a *null reference*? What is the difference between a *nested array* and a *multidimensional array*? etc.

Buoys lend themselves to illustrate notions like *variable*, *value*, *reference*, *equality*, *identity* etc. and to test a deeper understanding of them with problems of the form: "Draw the buoy(s) of the following variable(s) ...".

The term *exer* in this paper is meant to encompass everything which is used to execute a program (e.g. compilers, interpreters, operating systems, various kinds of hardware etc.). The *exer* also may be a human being (e.g. the reader) who executes a program with a pencil and paper.

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1. How to represent variables as buoys

The concept of a variable containing a value, which may be replaced by another value any number of times is arguably the most important and fundamental concept of most programming languages. Many phenomena pertaining to the realm of programming can only be comprehended with a precise mental image of how such a modifiable variable looks like. So-called **buoys** provide a graphical representation of variables, which supports and facilitates such a precise image. Variables of all mainstream programming languages can be represented by buoys. Buoys have been invented together with the programming language Algol 68 (towards the end of the nineteen-sixties) and have been slightly improved by students of the *Beuth University of Applied Sciences*. This paper is specifically about the programming language Java and its variables (and at the same time an introduction to buoys in general).

1.1. Types, variables and values in Java

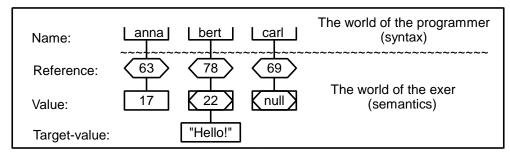
In Java it is useful to distinguish

Primitive types Reference types	(e.g. int, double, boolean,) and (e.g. String, List <string>, String[], String[][][],).</string>
	(i.e. variables of a primitive type) and (i.e. variables of a reference type),
Primitive values Reference values	(i.e. values which may be assigned to a primitive variable) and (i.e. values which may be assigned to a reference variable).

Example-01: One *primitive variable* and two *reference variables* represented as buoys:

```
1 int anna = 17;
2 StringBuilder bert = new StringBuilder("Hello!");
3 StringBuilder carl = null;
```

As buoys these three variables may look as follows:



Every variable consists of at least two parts: A **reference** and a **value**. Every variable may (or may not) have a **name**. In addition, reference variables may (or may not) have a **target-value**. Thus *primitive variables* may consist of 2 or 3 parts and *reference variables* may consist of 2, 3 or 4 parts.

Only the **name** of a variable (if present) belongs to the *world of the programmer*. The other parts belong to *the world of the exer*, because only he can generate and manipulate them, and the programmer will never see them directly (at most he may see certain shadows of values or target-values, e.g. on a screen).

	Canoe, for names	
$\langle \rangle$	Hexagon, for references	
	Rectangle, for values	1
	Rectangle plus hexagon, for values which are references	t t

In a buoy 4 geometric shapes are used to represent the (at most) 4 parts of a variable. **Names** are placed into so-called *canoes*. **Values** are enclosed in *rectangles*. **References** are enclosed in *hexagons*. The *value* of a reference variable is a *reference* and therefore is enclosed in a *rectangle* (as a value) and in a *hexagon* (as a reference). The special reference-value null does *not refer* to a target value. Every other reference-value *does* refer to a target value. In Java, every target value is an object.

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The exer may choose references any way he likes, as long as he guarantees two things:

- 1. References of variables are unique (i.e. different variables have different references).
- 2. The special value null is never used as the *reference* of a variable

(it is used only as the *value* of reference variables).

In Java, there are *no* operations which operate on the *references of variables*. And there are only *three* operations, which operate on *reference values*: == and != (the equality and the inequality operation, respectively) and = (the assignment operation). The programmer can not apply any other operation to reference values (e.g. he can **not** do a computation with them, convert them to an int-value or to a String-object or output them to the screen etc.).

Note: Even a program written in Jasmin (the assembler language for the Java Virtual Machine) can only compare reference values with == and != or assign them to a variable.

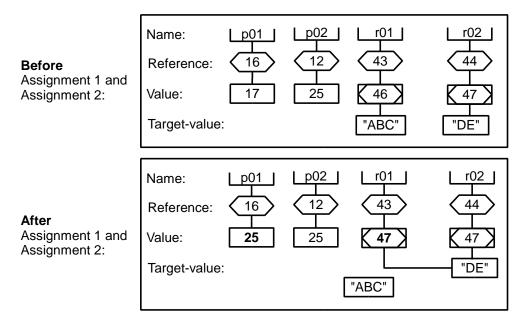
1.2. Assignment statements

An assignment statement of the form x = y; always copies the **value** of variable y into the value-box of variable x. This has radically different consequences depending on whether x and y are *primitive variables* or *reference variables*.

Example-02: Assignments between primitive variables vs. between reference variables

```
1 int p01 = 17;
2 int p02 = 25;
3 StringBuilder r01 = new StringBuilder("ABC");
4 StringBuilder r02 = new StringBuilder("DE");
5
6 p01 = p02; // Assignment 1 (between primitive variables)
7 r01 = r02; // Assignment 2 (between reference variables)
```

As buoys these 4 variables may look (before and after the assignments) as follows:



Remember: The *references* <16>, <12>, etc. and the *reference values* [<46>], [<47>] have been chosen by the exer following his particular taste.

After the assignment p01 = p02; the variables p01 and p02 have equal values (viz. 25 and 25). These values can be modified independently from each other (e.g. with additional assignments).

After the assignment r01 = r02; the variables r01 and r02 also have equal values (viz. [<47>] and [<47>]). With these values they refer to (one and) the *same* object (not to two *equal* objects!). If you change this object, you change the target-value of r01 and of r02.

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Problem-01: What is being output to the screen?

```
1 r01.append("XY"); // Appends "XY" to the target-value of r01
2 System.out.println(r02); // Outputs the target-value of r02
```

1.3. Different equals-methods

Every Java class contains an object method (a non-static method) with profile

public boolean equals(Object ob)

What this equals-method does (exactly when it will return true and when false) is decided by the programmer of the class in question, and therefore may vary widely from class to class.

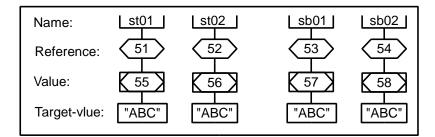
Example-03: equals-methods of classes String and StringBuilder

1 String st01 = new String("ABC"); 2 String st02 = new String("ABC"); 3 StringBuilder sb01 = new StringBuilder("ABC"); 4 StringBuilder sb02 = new StringBuilder("ABC");

new-rule: Each time it is called, the new-command returns a "new reference", which is different from all references existing so far. The new reference refers to a newly generated object and may be assigned to a reference variable (of the appropriate type) as its new value.

From this rule it follows, that the four variables st01, st02, sb01, sb02 are guaranteed to have four *different values* (because new has been called four times).

As buoys the four variables may look as follows:



Please note: The target-values of st01 and st02 are String-objects, whereas the target-values of sb01 and sb02 are StringBuilder-objects. The considerable differences between String-objects and StringBuilder-objects are not shown by the buoys (they have to be inferred from the context).

The programmer of class String has decided, that his equals-method compares *target-values* (i.e. String-objects), not the *values* of String-variables. From this it follows that the expression

st01.equals(st02)

evaluates to true (since "ABC" equals "ABC").

The programmer of class StringBuilder has decided, that his equals-method compares *values* of StringBuilder-variables, not *target-values*. From this it follows that the expression

sb01.equals(sb02)

evaluates to false (since [<57>] is not equal [<58>]).

End of Example-03.

To check, if two StringBuilder-variables refer to equal character sequences, you can convert their target-values (of type StringBuilder) to String-objects and then compare the String-objects, e.g. like that:

```
sb01.toString().equals(sb02.toString())
```

This expression evaluates to true (since "ABC" equals "ABC").

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Recommended: Before you compare objects of a class C with equals, you should read the documentation of C::equals (i.e. of the object-method equals of class C).

1.4. The one and only equality operation

The equality operation ==, when applied to variables, always compares their *values* and never their *names*, *references* or *target-values*.

Example-04: The operation ==

In this example, the variables defined in the previous example, are used.

The expression st01 == st02 evaluates to false (because [<55>] is not equal [<56>]) The expression sb01 == sb02 evaluates to false (because [<57>] is not equal [<58>])

To learn, what the *one* (and only) equality operation == does, is much easier than to learn what the *numerous* equals-methods are actually doing.

Sometimes a second operation is also called "an equality operation": !=. Its precise name is *inequality operation*. Whenever x == y throws an exception, x != y throws the same exception. In all other cases, x != y returns the value !(x == y). Thus, != comes close to be *the opposite* of ==.

1.5. Special rules for the type String

For each reference type there is a literal null. String is the only reference type, which has more than this null-literal: "ABC", "How are you?" and "" are examples of additional String-literals.

String-variables may therefore be initialized in two ways:

- with the new-command (like variables of other reference types)

- with a String-literal (and without new).

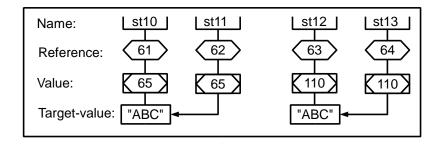
When a new-command is used, the **new-rule** applies ("each call of the new-command returns a new reference", see above).

StringLiteral-rule: All String-variables initialized with the same String-literal have *equal values* (and with these values refer to the *same* String-object).

Example-05: String-variables initialized with a literal only or with new:

```
1 String st10 = "ABC";
2 String st11 = "ABC";
3 String st12 = new String("ABC");
4 String st13 = st12;
```

As buoys these variables may look as follows:



The variables st10 and st11 have (following the **StringLiteral-rule**) equal values ([<65>] and [<65>]), because they are initialized with the same String-literal "ABC".

The variable st12 has (following the **new-rule**) a different value ([<110>]) than st10.

The variable st13 is initialized with the value of st12 (i.e. [<110>]). With this value st12 and st13 refer to the same "ABC"-object, but to a different "ABC"-object than st10 and st11.

2. How to represent arrays as buoys

The representation of variables by buoys can illustrate the structure of arrays and clarify (among other things) the following differences:

- between arrays with primitive elements and arrays with reference elements

- between nested arrays (native in Java) and multidimensional arrays (not native in Java)

- between an *empty array* and a null reference

2.1. Primitive or reference elements

An array of int contains int-variables. Those variables are located completely *inside* the array. An array of String contains String-variables, but the target-values of those variables (the String-objects) are located *outside* of the array (not inside). Thus:

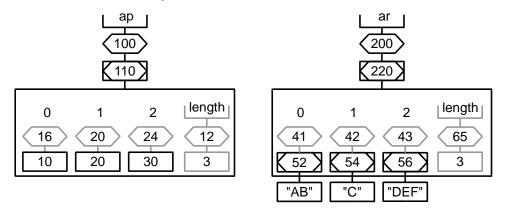
1. An "array of objects" does not really contain objects, but only references referring to objects.

2. An object may belong to any number of arrays at the same time (whereas a primitive value like 17 or true may belong to at most one array, other arrays may only contain copies of it).

Example-01: Two arrays represented by buoys:

5	int[]	ap	= -	{10, 20,	30}	;	//	An	array	with	primitive	elements
6	String[]	ar	=	{"AB", "(<u>;</u> ,	"DEF");	//	An	array	with	reference	elements

As buoys the variables ap and ar may look as follows:



Elaborate and abbreviated buoys: Buoys of Java arrays come in two forms: *elaborate* (as shown here) and *abbreviated* (if the gray parts are left out). Thus *references of array elements* are optional, as are all three parts of the variable length. Everything else is mandatory. The elaborate form is more realistic, the abbreviated form more convenient. We will use the convenient form most of the time.

The array element ap[0] is a *primitive variable* without a name (but we can refer to it with the expression ap[0]). Here this variable has the reference <16> and the value [10] and all its parts are located *within* the array ap (which is represented by a largish black rectangle).

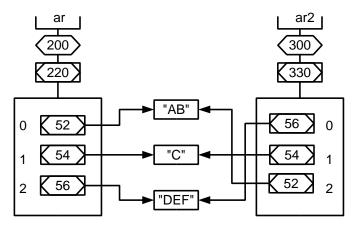
The array element ar[0] is a *reference variable* without a name (but we can refer to it with the expression ar[0]). Here this variable has the reference <41>, the value [<52>] and the target-value ["AB"]. Note, that the target-value is located *outside* the rectangle of the array ar.

Remember: All *references* like <16>, <20>, ... etc. and all *reference values* like [<52>], [<54>], ... etc. have been chosen by the exer following his particular taste (do not question his taste! :-).

The array object ar (the target-value of the variable ar) contains 3 elements and additionally an intvariable named length with value 3. In all arrays this length-variable is *unmodifiable*.

The buoy of ar should make it clear, that the array does not contain String-objects, but only *references* that refer to such objects. Thus it is possible, that the same String-object (which may be very large) belongs to several arrays at the same time, being represented in each array only by a (relatively small) reference value.

Example-02: Two arrays "containing" the same String-objects (buoys in abbreviated form):



The array ar "contains" 3 String-objects, sorted in ascending order ("AB", "C", "DEF"). The array ar2 "contains" the same 3 String-objects, sorted in descending order ("DEF", "C", "AB").

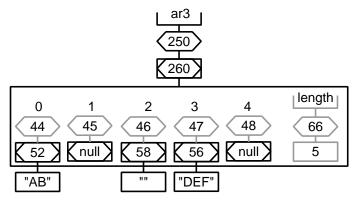
In this example the three String-objects are rather small. But if each of them had a size of 1MB, the two arrays ar and ar2 together would not occupy 6 MB of memory, but only slightly more than 3 MB.

An array with elements of a *reference type* may contain null-elements. Such elements do *not* refer to any target-value.

Example-03: An array with 2 null-elements and an empty-String-element

7 String[] ar3 = {"AB", null, "", "DEF", null);

As a buoy (in elaborate form) ar 3 may look as follows:



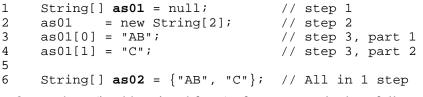
A null-element (like e.g. ar3[1] or ar3[4]) is fundamentally different from an empty String-object (like e.g. ar3[2]). A null-element does not refer to a target-value. But even an empty Stringobject is a full-blown object, which contains more than 60 methods. Only the number of characters it contains is the smallest possible (i.e. 0).

Analogy: To have an *empty cup of coffee* is different from having *no cup* at all.

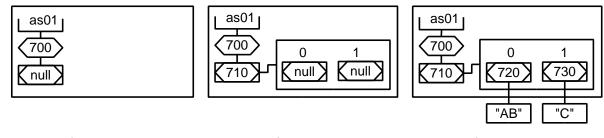
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2.2. Constructing an array in 3 steps or in 1 step

The following sequence of commands will first construct an array as01 in 3 steps, and then a very similar array as02 in a single step. The 3-step-construction will be illustrated with 3 snapshots, i.e. buoys, that show how as01 looks after each step.



The 3 snapshots (in abbreviated form) of as01 may look as follows:



after step 1

after step 2

after step 3

After step 1: There is an array variable as01 (which *may* refer to an array), but no array yet.

After step 2: Now the array variable as01 refers to an array, but the array contains only null-elements.

After step 3: Now the array elements refer to String-objects

Problem-02: Draw as02 as buoy. Which parts are equal to those of as01 and which parts are guaranteed to differ?

2.3. Nested arrays

Nesting-Rule-1: For every type T there is an *array type* T[] (pronounced: array of T) and T is called the *element type* of the array type T[].

In Java every array type (and every array) has a *nesting depth*. This depth is equal to the number of pairs of square brackets [] in the type name.

Array type	pronounced	nesting depth	Element type
int[]	array of int	1	int
int[][]	array of arrays of int	2	int[]
int[][][]	array of arrays of arrays of int	3	int[][]
String[]	array of String	1	String
String[][]	array of arrays of String	2	String[]
String[][][]	array of arrays of arrays of String	3	String[][]

Example-01: Some array types, their pronunciation, nesting depth and element type

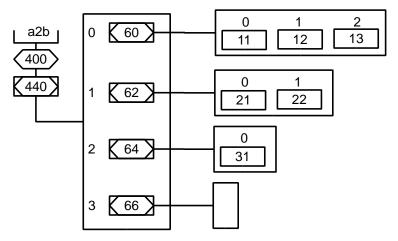
Def.: A **nested array** is an array with nesting depth 2 or greater. Arrays with a nesting depth of 1 are sometimes called *non-nested*.

Example-02: Nested arrays, and a buoy for one of them:

1 int[][] a2a = {{11, 12, 13}, {21, 22, 23}, {31, 32, 33}}; 2 int[][] a2b = {{11, 12, 13}, {21, 22}, {31}, {};

The array a2a has 3 elements of type int[] (and indirectly contains 9 int-elements).

The array a2b has 4 elements of type int[] (and indirectly contains 6 int-elements). As a buoy (in abbreviated form) the array a2b may look as follows:



This example shows, that the elements of a nested array may be (arrays) of different lengths.

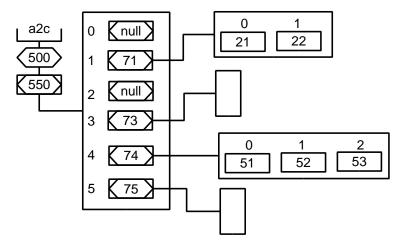
Remember: An array of objects does not really contain objects, but only references, which refer to objects. A nested array is an array of array-objects. Therefore it does not contain array-objects as its elements, but references, which refer to array-objects.

Problem-03: Draw a buoy (in abbreviated or in elaborate form, as you like) which represents the array variable a2a of **Example-02**.

Besides "plain vanilla elements" a nested array may contain elements of more exciting flavors too .

Example-03: A nested array with *empty elements* and null-*elements*:

3 int[][] **a2c** = {null, {21, 22}, null, {}, {51, 52, 53}, {}}; As a buoy (in abbreviated form), the array variable a2c may look as follows:



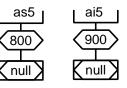
The array a2c contains six elements, of which two are empty arrays (a2c[3] and a2c[5]) and two are null-elements (a2c[0] and a2c[2]).

2.4. Nested arrays and new-commands

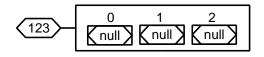
The following declarations

1 string[][][][] as5 = null; 2 int[][][][] ai5 = null;

tell the exer to create 2 variables. As buoys these variables may look like shown on the right. Although the declaration contains a generous amount of square brackets, the buoys look like any other reference variable. But they have a hidden special trait, which is not represented in the buoys, but is well known to the exer.



The values of as5 and ai5 seem to be equal, since they both are represented by null. But in reality, these null-values are of different types and thus incomparable (an expression like as5 == ai5 would be a syntax error). The null-value of as5 is of the type String[][][][][], whereas the null-value of ai5 is of type int[][][][].



The following new-command:

... new String[3][][][][] ...

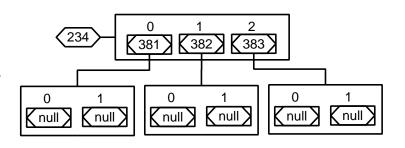
generates an array of nesting depth 1, which as a buoy may look like shown on the left, and returns a reference, which

refers to this array (here this is the reference <123>). This reference is of type String[][][][]] and thus may be assigned to the variable as5: as5 = new String[3][][][];

The new-command ... new int[3][][][] ... generates a very similar array and returns a reference referring to it. That reference is of type int[][][][] and therefor may be assigned to ai5: ai5 = new int[3][][][][];

Problem-04: Of which type are the null-elements in the array referred to by the reference <123>?

The following new-command ... new int[3][2][] ... generates an array with nesting depth 2 as shown on the right, and returns a reference, which refers to this array (here: <234>). This reference is of type int[][]. The null-elements in the element arrays are all of type int[].



Problem-05: The following new-command will return a reference R

referring to to a newly generated array A:

... new int[2][5][3][][][] ...

- 1. Of what type is R?
- 2. What depth of nesting does A have?

3. At its bottom the array A will contain some null-values. Of which type are they?

2.5. Sometimes nesting is for the birds

For a mathematician, it's an easy exercise to regard *all objects* as arrays. Using an old trick he would call an object, which really is not an array, "an array of nesting depth 0". And he would proudly point out, that with this funny way of speaking the following simple rule would make sense:

Nesting-rule-2: An array has nesting depth n, if all its elements have nesting depth n-1.

Self-evident as this rule may sound: In some cases it fails to work.

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How to represent arrays as buoys

Example-01: An array with a dubious depth of nesting

```
1 String vs = "Hello!"; // depth of nesting: 0
2 String[] as = {"A", "B"}; // depth of nesting: 1
3 int[][] ai = {{11, 12}, {21, 22}}; // depth of nesting: 2
4
5 Object[] ao1 = {as, ai, vs}; // depth of nesting?
```

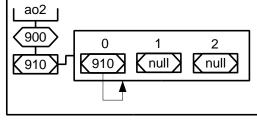
In this example, the array aol is the culprit. It contains as its elements arrays of different depths of nesting. Therefore, its own depth is not defined by **Nesting-rule-2**.

Even worse: An array of type Object[] may contain any array as element, *even itself*.

Example-02: An array which contains itself as an element

```
1 Object[] ao2 = new Object[3];
2 ao2[0] = ao2;
```

The **Nesting-rule-2** does not define a nesting depth for the array ao2.



2.6. Multidimensional arrays

Apparently, many people are against discrimination, even against discrimination between *nested arrays* and *multidimensional arrays*. This is unfortunate, because the difference between them is interesting and of practical relevance. Roughly speaking: Nested arrays are more powerful (they can solve more problems), but multidimensional arrays (if applicable) are more efficient (they need less memory and execution time).

There is no difference between *non-nested arrays* (with a nesting depth of 1) and *1-dimensional arrays*. But nested arrays (with a nesting depth of 2 or greater) and truly multidimensional arrays (with 2 or more dimensions) are different creatures.

Arrays in Java are nested (or: arrays of arrays, not multidimensional) (see p. 4 of https://docs.oracle.com/javase/specs/jls/se8/jls8.pdf).

In Fortran and Pascal, there are only multidimensional arrays. In Ada, C++ and C#, both nested and multidimensional arrays are native features.

The important differences between the two kinds of arrays:

A nested array contains arrays, which may be of different lengths.

A *multidimensional array* does not contain arrays, but elements of a non-array-type (like int, float, String, ... etc.). To access an element, one needs to supply several indices, one for each dimension, e.g. mar[3, 5] would access the element in the 3rd line and 5th column of a 2-dimensional array mar.

A multidimensional array has a fixed length for each of its dimensions. E.g. a 2-dimensional array may consist of 10 lines of 15 rows each (all lines have to have the same length). A 5-dimensional array has to "resemble" the shape of a 5-dimensional cuboid.

A nested array is usually implemented as an *array of references* (which refer to arrays). A multidimensional array is usually implemented as a non-nested (or: 1-dimensional) array plus some fancy index-fiddling.

People at IBM have extended Java by some commands for the generation and handling of multidimensional arrays (see <u>http://researcher.watson.ibm.com/researcher/files/us-bacon/Bacon98JaLA.pdf</u>), but these extensions require a special IBM-Java-compiler.

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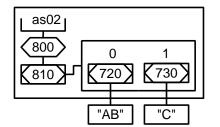
3. Solutions for the Problems

Solution for Problem-01: What is being output to the screen?

```
1 r01.append("XY"); // Appends "XY" to the target-value of r01
2 System.out.println(r02); // Outputs the target-value of r02
```

Output: DEXY

Solution for Problem-02: Draw as02 as buoy. Which parts are equal to those of as01 and which parts are guaranteed to differ?



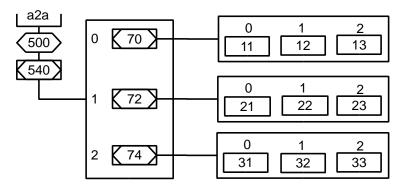
The reference <800> and value [<810>] of as02 are guaranteed to be different from those of as01.

The values [<720>] and [<720>] of as02[0] and as02[1] are guaranteed to equal the values of as01[0] and as01[1].

Solution for Problem-03: Draw a buoy (in abbreviated or in elaborate form, as you like) which represents the array variable a2a of **Example-02**.

1 int[][] **a2a** = {{11, 12, 13}, {21, 22, 23}, {31, 32, 33}};

The array variable a2a in abbreviated form:



Solution for Problem-04: Of which type are the null-elements in the array referred to by the reference <123>?

They are of type int[][][][].

Solution for Problem-05: The following new-command will return a reference R referring to to a newly generated array A:

... new int[2][5][3][][][] ...

1. Of what type is R?

2. What depth of nesting does A have?

Of type int[][][]] A has nesting depth 3

3. At its bottom the array A will contain some null-values. Of which type are they?

They are of type int[][]